

Math 210, Lec. 3, Fall 1999

NAME:

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Discussion Day&Time:

EXAM 2, October 15, 1999

SCORE:

Some Formulas:

$$Pr[E|F] = Pr[E \cap F]/Pr[F], P(n, r) = n!/(n-r)!, C(n, r) = n!/r!(n-r)!$$

$$\mu = E[X] = x_1p_1 + \dots + x_kp_k, Var[X] = (x_1 - \mu)^2p_1 + \dots + (x_k - \mu)^2p_k, \sigma = \sqrt{V(X)}$$

$$C(n, r)p^r(1-p)^{n-r}, \mu = E[X] = np, Var[X] = np(1-p), \sigma[X] = \sqrt{np(1-p)}$$

NOTE: There are four major questions I, III, II, IV. Answers need not be computed unless needed to answer a subsequent question. Answers given as a number (e.g. 720) with no indication of the reasoning involved are not acceptable.

I. 25 points A test for a "Really Awful Disease" (abbreviated RAD) can sometimes give a *false-positive* result (this happens when a person does not have RAD but the test result is positive). The test can also give a negative result when a person does have RAD. Suppose that the probabilities for the results of this test on a random person are:

	positive	negative
person with RAD	.95	.05
person without RAD	.15	.85

Suppose 8% of the people in a community have RAD. If a person is selected at random and tests positive, what is the probability that she has RAD?

**II. 25 points** There are two containers, a **bag** and a **box**. The **bag** contains 5 Red and 3 Blue Balls and the **box** contains 2 Red and 5 Blue Balls. A stochastic process consists of (i) selecting at random one of the containers, (ii) picking a ball at random from the selected container, noting its color, and putting it in the other container. (iii) selecting a ball from the other container.

(a) Draw a tree diagram labeling the branches with the appropriate probabilities.

(b) Determine the probability of the event that the two balls selected have different colors.

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III. 25 points Consider the game whereby a person chooses at random a pair of **distinct** numbers (two at the same time) from 1, 2, 3, 4, 5, 6, 7, 8, 9. If both numbers are odd, the player gets \$5; if both are even, she gets \$4; if one is even and one is odd, she loses \$4. Let  $X$  be the random variable which gives the player's payoff.

(a) Determine the expected value of  $X$ .

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(b) Is it wise for the player to play this game? Why or why not?

**IV. 25 points** A bag contains 3 Red and 4 Blue balls. Six balls are drawn at random in succession and with replacement. Find:

(a) The probability that an odd number of Red balls are drawn:

(b) The probability that at least one ball of each color is drawn:

(c) The expected number of Red balls drawn when six balls are drawn as described above.

(d) The variance for this experiment.